Automated Exercises for	Automated Exercises - Why?
Constraint Programming	<ul> <li>lecture without homework exercises is useless</li> </ul>
Johannes Waldmann (HTWK Leipzig)	<ul> <li>homework that is not discussed/graded is useless</li> </ul>
	<ul> <li>no money to pay teaching assistants for grading</li> </ul>
http://www.imn.htwk-leipzig.de/	<ul> <li>not enough time to discuss everything in class</li> </ul>
~waldmann/talk/14/wlp/auto/	<ul> <li>automated and real-time grading helps student to understand the basics</li> </ul>
September 16, 2014	<ul> <li>and frees class time for more interesting discussion</li> </ul>
(Declarative) Constr. Programming	Exercise for Propositional SAT
<ul> <li>constraint program (w.r.t. structure S) is formula F in predicate logic</li> </ul>	(to show the general idea in a very straigthforward case)
► constraint <i>solver</i> answers the question <i>F</i> ∈ Theory( <i>S</i> )	<ul> <li>exercise</li> <li>instance: satisfiable formula F (in CNF)</li> </ul>
In particular, if F is of shape ∃x <sub>1</sub> ,, x <sub>n</sub> : M, by giving a satisfying assignment	<ul> <li>solution: a satisfying assignment</li> <li>generator</li> <li>will produce random satisfiable F</li> </ul>
<ul><li>aspects for teaching:</li><li>(syntax and semantics of predicate logic)</li></ul>	<ul> <li>with given number of variables and clauses</li> </ul>
<ul> <li>model application problems by constraints</li> </ul>	<ul> <li>doing the exercise, student will</li> <li>(learn semantics of propositional formulas)</li> </ul>
<ul> <li>explain how solvers work</li> <li>Kroening, Strichman: <i>Decision Procedures</i> (Springer, 2008)</li> </ul>	<ul> <li>appreciate the "hard work" that the SAT solvers do</li> </ul>
UNSAT proofs by resolution	A general model for automated exercises
exercise:	doing the exercise, student has to make choices general description (analogy)
<ul> <li>instance: unsatisfiable F in CNF</li> <li>solution: a resolution proof of the empty</li> </ul>	<ul> <li>exercise: non-deterministic algorithm</li> </ul>
clause actually,	<ul> <li>student: acts as oracle</li> <li>automated grader: acts as verifier</li> </ul>
<ul> <li>proof is DAG, represented as list of nodes</li> <li>root nodes are clauses from F</li> </ul>	<ul><li>how does this fit the teaching objetives?</li><li>if the subject is NP, then very well</li></ul>
<ul> <li>each internal node is resolution step</li> </ul>	<ul><li>(obviously)</li><li>if the subject is a deterministic algorithm (as</li></ul>
	used in constraint solvers), then what?
Exercises for Decision Methods	Exercise for solving FD constraints
<ul> <li>present the (invariants of the) algorithm via inference rules,</li> </ul>	via tree search, state is given by stack of domain assignments (variable $\mapsto$ subset of domain)
as in (e.g.) Apt: Principles of Constraint Programming	<ul> <li>Decide: for variable, pick value, push others</li> <li>Solved, Backtrack, Inconsistent</li> </ul>
<ul> <li>most often these rules are non-deterministic in a natural way</li> </ul>	$\frac{x \in D}{x = a \mid x \in D \setminus \{a\}} \text{ for } a \in D$
<ul> <li>this allows to apply our exercise model</li> <li>concrete algorithm corresponds to specific</li> </ul>	Stack [listToFM [(x, [0,1,2,3]), (y, [0,3])]]
<ul> <li>strategy in rule applications</li> <li>strategy is ignored in verifying the solutions</li> </ul>	== Decide x 1 ==>
<ul> <li>strategy is ignored in verifying the solutions</li> <li>but can be enforced implicitly (using wrong strategy takes too many steps)</li> </ul>	Stack [listToFM [(x, [ 1 ]), (y, [0,3])] ,listToFM [(x, [0, 2,3]), (y, [0,3])] ]

<pre>Ex. for FD: Arc Consistency ( P , mkSet     [ [ 0, 0, 0 ], [ 0, 1, 1 ], [ 0, 2, 2 ]     , [ 0, 3, 3 ], [ 1, 0, 1 ], [ 1, 1, 2 ]     , [ 1, 2, 3 ], [ 2, 0, 2 ], [ 2, 1, 3 ]     , [ 3, 0, 3 ] ] ) current : Stack [ listToFM [ ( x, [ 0 ] )</pre>	<ul> <li>FD constraints (Exercise design) if constraint is unsat, then</li> <li>student has to produce a full search tree</li> <li>could be done by Decide/Backtrack only, but is impractical</li> <li>enforces the usage of arc consistency deductions</li> <li>if constraint is sat, then</li> <li>student could guess a solution</li> <li>and then just enter the corresponding Decide-steps (and avoid arc consistency considerations)</li> <li>Decide must always uses lowest value</li> </ul>
<ul> <li>Exercise for DPLL with CDCL</li> <li>Davis, Putnam, Logeman, Loveland, solves SAT</li> <li>plain DPLL: just like FD tree search, unit propagation ≈ 1-consistency.</li> <li>Conflict Driven Clause Learning, Backjumping in case of conflict:</li> <li>learn a new clause <i>R</i> (the conflict "reason", must be inferrable from clauses used to obtain current assignment)</li> <li>jump back (and use <i>R</i> for unit propagation) student choices: what to learn, where to jump</li> </ul>	<ul> <li>DPLL Exercise Generator naive approach:</li> <li>since DPLL is complete method, it can be applied to <i>any</i> formula</li> <li>drawback: solutions (proof traces) vary greatly in length</li> <li>fair approach:</li> <li>generate formula</li> <li>find (shortest) proof trace (implement backtracking solver)</li> <li>choose formula where proof trace length is reasonable</li> <li>drawback: source code contains solver, students may exploit this</li> </ul>
SAT and DPLL modulo Theory Syntax: F in CNF where clauses may contain• Boolean literals and • theory literals, e.g., $\neg(2x + 3 > 4y)$ state of search given by partial assigment (= set of literals) $\sigma$ two kinds of conflicts: • Boolean conflict (F contains clause where all literals are false in $\sigma$ ) • Theory conflict (theory literals from $\sigma$ are inconsistent)example: • Theory of linear inequalities (over $\mathbb{Q}$ ) • Solver: Fourier-Motzkin	<ul> <li>Conclusion, Discussion</li> <li>exercises for constraint programming</li> <li>automated generation of instances, grading of solutions</li> <li>use exercises (anonymously) at https: //autotool.imn.htwk-leipzig.de/cgi-bin/Trial.cgi?lecture=199</li> <li>make our own autotool installation (run it in a VM, https://github.com/marcellussiegburg/autobuildtool)</li> </ul>